

Data-scientific software for the surface structure analysis by total-reflection high-energy positron diffraction (TRHEPD)

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The data scientific software was developed for the surface structure analysis by the total-reflection high-energy positron diffraction (TRHEPD). The experiment has been intensively conducted at the Slow Positron Facility (SPF), Institute of Materials Structure Science (IMSS), High Energy Accelerator Research Organization (KEK) and revealed the structure of the surfaces of interest [1].

The present paper reports the recent activity of the software development for the data analysis of TRHEPD. It is based on the inverse problem in which the atomic positions $X = (X_1, X_2, \dots, X_N)$ of a surface structure are determined from the experimental diffraction data (rocking curve) D_{exp} ($D_{\text{exp}} \Rightarrow X$). The forward problem ($X \Rightarrow D_{\text{cal}}(X)$) is solved, for many trial atomic positions X , by the numerical solution of the partial differential equation in quantum scattering problem [2]. The R-factor $R(X) = |D_{\text{cal}}(X) - D_{\text{exp}}|$, the residual error between the experimental and calculated diffraction data, is minimized as a function of the atomic position. Two possible methods are considered; one is the local search procedure by the gradient-free optimization (Nelder–Mead) method and the other is the global search procedure by the grid or stochastic sampling (Monte Carlo) method. The global search procedure requires a large computational cost and is realized on supercomputers with parallel computation.

This presentation demonstrates the application of the method to several known surface structures, as preliminary attempts. Our data-scientific approach is general and applicable to other experiments also, like Low Energy Electron Diffraction (LEED), when one replaces the forward problem solver. The program code is written mainly in the Python language and will be available online in near future.

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